

Lower Township Elementary School District

Math

Grade 3



Curriculum

Adopted by the Lower Township Board of Education on August 29, 2017

Lower Township Elementary School District

Course Description:

In Grade 3, instructional time should focus on four critical areas: developing understanding of multiplication and division and strategies for multiplication and division within 100; developing understanding of fractions, especially unit fractions (fractions with numerator 1); developing understanding of the structure of rectangular arrays and of area; and describing and analyzing two-dimensional shapes.

Students develop an understanding of the meanings of multiplication and division of whole numbers through activities and problems involving equal-sized groups, arrays, and area models; multiplication is finding an unknown product, and division is finding an unknown factor in these situations. For equal-sized group situations, division can require finding the unknown number of groups or the unknown group size. Students use properties of operations to calculate products of whole numbers, using increasingly sophisticated strategies based on these properties to solve multiplication and division problems involving single-digit factors. By comparing a variety of solution strategies, students learn the relationship between multiplication and division.

Students develop an understanding of fractions, beginning with unit fractions. Students view fractions in general as being built out of unit fractions, and they use fractions along with visual fraction models to represent parts of a whole. Students understand that the size of a fractional part is relative to the size of the whole. For example, $\frac{1}{2}$ of the paint in a small bucket could be less paint than $\frac{1}{3}$ of the paint in a larger bucket, but $\frac{1}{3}$ of a ribbon is longer than $\frac{1}{5}$ of the same ribbon because when the ribbon is divided into 3 equal parts, the parts are longer than when the ribbon is divided into 5 equal parts. Students are able to use fractions to represent numbers equal to, less than, and greater than one. They solve problems that involve comparing fractions by using visual fraction models and strategies based on noticing equal numerators or denominators.

Students recognize area as an attribute of two-dimensional regions. They measure the area of a shape by finding the total number of same size units of area required to cover the shape without gaps or overlaps, a square with sides of unit length being the standard unit for measuring area. Students understand that rectangular arrays can be decomposed into identical rows or into identical columns. By decomposing rectangles into rectangular arrays of squares, students connect area to multiplication, and justify using multiplication to determine the area of a rectangle.

Students describe, analyze, and compare properties of two-dimensional shapes. They compare and classify shapes by their sides and angles, and connect these with definitions of shapes. Students also relate their fraction work to geometry by expressing the area of part of a shape as a unit fraction of the whole.

Lower Township Elementary School District

Course Goals:

- A. Operations and Algebraic Thinking – 3.OA
- Represent and solve problems involving multiplication and division.
 - Understand properties of multiplication and the relationship between multiplication and division.
 - Multiply and divide within 100.
 - Solve problems involving the four operations, and identify and explain patterns in arithmetic.
- B. Number and Operations in Base Ten – 3.NBT
- Use place value understanding and properties of operations to perform multi-digit arithmetic.
- C. Number and Operations—Fractions – 3.NF
- Develop understanding of fractions as numbers.
- D. Measurement and Data – 3.MD
- Solve problems involving measurement and estimation of intervals of time, liquid volumes, and masses of objects.
 - Represent and interpret data.
 - Geometric measurement: understand concepts of area and relate area to multiplication and to addition.
 - Geometric measurement: recognize perimeter as an attribute of plane figures and distinguish between linear and area measures.
- E. Geometry – 3.G
- Reason with shapes and their attributes.

Lower Township Elementary School District

Course Enduring Understandings:

Ideas that have lasting value beyond the classroom. Consider, “what do we want students to understand and be able to use several years from now, after they have forgotten the details?”

A. Operations and Algebraic Thinking – 3.OA

- Mathematical operations are used in solving problems in which a new value is produced from one or more values.
- Algebraic thinking involves choosing, combining, and applying effective strategies for answering quantitative questions.

B. Number and Operations in Base Ten – 3.NBT

- Understanding place value can lead to number sense and efficient strategies for computing with numbers.

C. Number and Operations—Fractions – 3.NF

- Fractions and decimals allow for quantities to be expressed with greater precision than with just whole numbers.

D. Measurement and Data – 3.MD

- Measurement processes are used in everyday life to describe and quantify the world.
- Data displays describe and represent data in alternative ways.

E. Geometry – 3.G

- Geometric attributes (such as shapes, lines, angles, figures, and planes) provide descriptive information about an object’s properties and position in space and support visualization and problem solving.

Lower Township Elementary School District

Lower Township Elementary School District

NJSLS- MATH:

Grade 3 Overview

Operations and Algebraic Thinking

- Represent and solve problems involving multiplication and division.
- Understand properties of multiplication and the relationship between multiplication and division.
- Multiply and divide within 100.
- Solve problems involving the four operations, and identify and explain patterns in arithmetic.

Number and Operations in Base Ten

- Use place value understanding and properties of operations to perform multi-digit arithmetic.

Number and Operations—Fractions

- Develop understanding of fractions as numbers.

Measurement and Data

- Solve problems involving measurement and estimation of intervals of time, liquid volumes, and masses of objects.
- Represent and interpret data.
- Geometric measurement: understand concepts of area and relate area to multiplication and to addition.
- Geometric measurement: recognize perimeter as an attribute of plane figures and distinguish between linear and area measures.

Geometry

- Reason with shapes and their attributes.

Mathematical Practices

1. Make sense of problems and persevere in solving them.
2. Reason abstractly and quantitatively.
3. Construct viable arguments and critique the reasoning of others.
4. Model with mathematics.
5. Use appropriate tools strategically.
6. Attend to precision.
7. Look for and make use of structure.
8. Look for and express regularity in repeated reasoning.

Lower Township Elementary School District

Operations and Algebraic Thinking

3.OA

Represent and solve problems involving multiplication and division.

1. Interpret products of whole numbers, e.g., interpret 5×7 as the total number of objects in 5 groups of 7 objects each. *For example, describe a context in which a total number of objects can be expressed as 5×7 .*
2. Interpret whole-number quotients of whole numbers, e.g., interpret $56 \div 8$ as the number of objects in each share when 56 objects are partitioned equally into 8 shares, or as a number of shares when 56 objects are partitioned into equal shares of 8 objects each. *For example, describe a context in which a number of shares or a number of groups can be expressed as $56 \div 8$.*
3. Use multiplication and division within 100 to solve word problems in situations involving equal groups, arrays, and measurement quantities, e.g., by using drawings and equations with a symbol for the unknown number to represent the problem.¹
4. Determine the unknown whole number in a multiplication or division equation relating three whole numbers. *For example, determine the unknown number that makes the equation true in each of the equations $8 \times ? = 48$, $5 = \square \div 3$, $6 \times 6 = ?$.*

Understand properties of multiplication and the relationship between multiplication and division.

5. Apply properties of operations as strategies to multiply and divide.² *Examples: If $6 \times 4 = 24$ is known, then $4 \times 6 = 24$ is also known. (Commutative property of multiplication.) $3 \times 5 \times 2$ can be found by $3 \times 5 = 15$, then $15 \times 2 = 30$, or by $5 \times 2 = 10$, then $3 \times 10 = 30$. (Associative property of multiplication.) Knowing that $8 \times 5 = 40$ and $8 \times 2 = 16$, one can find 8×7 as $8 \times (5 + 2) = (8 \times 5) + (8 \times 2) = 40 + 16 = 56$. (Distributive property.)*
6. Understand division as an unknown-factor problem. *For example, find $32 \div 8$ by finding the number that makes 32 when multiplied by 8.*

Multiply and divide within 100.

7. Fluently multiply and divide within 100, using strategies such as the relationship between multiplication and division (e.g., knowing that $8 \times 5 = 40$, one knows $40 \div 5 = 8$) or properties of operations. By the end of Grade 3, know from memory all products of two one-digit numbers.

Solve problems involving the four operations, and identify and explain patterns in arithmetic.

8. Solve two-step word problems using the four operations. Represent these problems using equations with a letter standing for the unknown quantity. Assess the reasonableness of answers using mental computation and estimation strategies including rounding.³
9. Identify arithmetic patterns (including patterns in the addition table or multiplication table), and explain them using properties of operations. *For example, observe that 4 times a number is always even, and explain why 4 times a number can be decomposed into two equal addends.*

Lower Township Elementary School District

Number and Operations in Base Ten

3.NBT

Use place value understanding and properties of operations to perform multi-digit arithmetic.⁴

1. Use place value understanding to round whole numbers to the nearest 10 or 100.
2. Fluently add and subtract within 1000 using strategies and algorithms based on place value, properties of operations, and/or the relationship between addition and subtraction.
3. Multiply one-digit whole numbers by multiples of 10 in the range 10–90 (e.g., 9×80 , 5×60) using strategies based on place value and properties of operations.

Number and Operations—Fractions⁵

3.NF

Develop understanding of fractions as numbers.

1. Understand a fraction $1/b$ as the quantity formed by 1 part when a whole is partitioned into b equal parts; understand a fraction a/b as the quantity formed by a parts of size $1/b$.
2. Understand a fraction as a number on the number line; represent fractions on a number line diagram.
 - a. Represent a fraction $1/b$ on a number line diagram by defining the interval from 0 to 1 as the whole and partitioning it into b equal parts. Recognize that each part has size $1/b$ and that the endpoint of the part based at 0 locates the number $1/b$ on the number line.
 - b. Represent a fraction a/b on a number line diagram by marking off a lengths $1/b$ from 0. Recognize that the resulting interval has size a/b and that its endpoint locates the number a/b on the number line.
3. Explain equivalence of fractions in special cases, and compare fractions by reasoning about their size.
 - a. Understand two fractions as equivalent (equal) if they are the same size, or the same point on a number line.
 - b. Recognize and generate simple equivalent fractions, e.g., $1/2 = 2/4$, $4/6 = 2/3$. Explain why the fractions are equivalent, e.g., by using a visual fraction model.
 - c. Express whole numbers as fractions, and recognize fractions that are equivalent to whole numbers. *Examples: Express 3 in the form $3 = 3/1$; recognize that $6/1 = 6$; locate $4/4$ and 1 at the same point of a number line diagram.*
 - d. Compare two fractions with the same numerator or the same denominator by reasoning about their size. Recognize that comparisons are valid only when the two fractions refer to the same whole. Record the results of comparisons with the symbols $>$, $=$, or $<$, and justify the conclusions, e.g., by using a visual fraction model.

Measurement and Data

3.MD

Solve problems involving measurement and estimation of intervals of time, liquid volumes, and masses of objects.

1. Tell and write time to the nearest minute and measure time intervals in minutes. Solve word problems involving addition and subtraction of time intervals in minutes, e.g., by representing the problem on a number line diagram.

Lower Township Elementary School District

2. Measure and estimate liquid volumes and masses of objects using standard units of grams (g), kilograms (kg), and liters (l).⁶ Add, subtract, multiply, or divide to solve one-step word problems involving masses or volumes that are given in the same units, e.g., by using drawings (such as a beaker with a measurement scale) to represent the problem.⁷

Represent and interpret data.

3. Draw a scaled picture graph and a scaled bar graph to represent a data set with several categories. Solve one- and two-step "how many more" and "how many less" problems using information presented in scaled bar graphs. *For example, draw a bar graph in which each square in the bar graph might represent 5 pets.*
4. Generate measurement data by measuring lengths using rulers marked with halves and fourths of an inch. Show the data by making a line plot, where the horizontal scale is marked off in appropriate units—whole numbers, halves, or quarters.

Geometric measurement: understand concepts of area and relate area to multiplication and to addition.

5. Recognize area as an attribute of plane figures and understand concepts of area measurement.
 - a. A square with side length 1 unit, called "a unit square," is said to have "one square unit" of area, and can be used to measure area.
 - b. A plane figure which can be covered without gaps or overlaps by n unit squares is said to have an area of n square units.
6. Measure areas by counting unit squares (square cm, square m, square in, square ft, and improvised units).
7. Relate area to the operations of multiplication and addition.
 - a. Find the area of a rectangle with whole-number side lengths by tiling it, and show that the area is the same as would be found by multiplying the side lengths.
 - b. Multiply side lengths to find areas of rectangles with whole-number side lengths in the context of solving real world and mathematical problems, and represent whole-number products as rectangular areas in mathematical reasoning.
 - c. Use tiling to show in a concrete case that the area of a rectangle with whole-number side lengths a and $b + c$ is the sum of $a \times b$ and $a \times c$. Use area models to represent the distributive property in mathematical reasoning.
 - d. Recognize area as additive. Find areas of rectilinear figures by decomposing them into non-overlapping rectangles and adding the areas of the non-overlapping parts, applying this technique to solve real world problems.

Geometric measurement: recognize perimeter as an attribute of plane figures and distinguish between linear and area measures.

8. Solve real world and mathematical problems involving perimeters of polygons, including finding the perimeter given the side lengths, finding an unknown side length, and exhibiting rectangles with the same perimeter and different areas or with the same area and different perimeters.

Lower Township Elementary School District

Geometry

3.G

Reason with shapes and their attributes.

1. Understand that shapes in different categories (e.g., rhombuses, rectangles, and others) may share attributes (e.g., having four sides), and that the shared attributes can define a larger category (e.g., quadrilaterals). Recognize rhombuses, rectangles, and squares as examples of quadrilaterals, and draw examples of quadrilaterals that do not belong to any of these sub-categories.
2. Partition shapes into parts with equal areas. Express the area of each part as a unit fraction of the whole. *For example, partition a shape into 4 parts with equal area, and describe the area of each part as $\frac{1}{4}$ of the area of the shape.*

Lower Township Elementary School District

21st Century Career Ready Practices:

Career Ready Practices	
1. Act as a responsible and contributing citizen and employee.	X
2. Apply appropriate academic and technical skills	X
3. Attend to personal health and financial well-being.	X
4. Communicate clearly and effectively and with reason.	X
5. Consider the environmental, social and economic impacts of decisions	X
6. Demonstrate creativity and innovation.	X
7. Employ valid and reliable research strategies.	X
8. Utilize critical thinking to make sense of problems and persevere in solving them.	X
9. Model integrity, ethical leadership and effective management.	X
10. Plan education and career paths aligned to personal goals.	X
11. Use technology to enhance productivity.	X
12. Work productively in teams while using cultural global competence.	X

21st Century Life and Careers Standards Addressed/Taught in 3rd Grade Math

9.1.4.B.1	Differentiate between financial wants and needs
9.1.4.D.1	Determine various ways to save.
9.1.8.E.1	Explain what it means to be a responsible consumer and the factors to consider when making consumer decisions.
9.2.4.A.4	Explain why knowledge and skills acquired in the elementary grades lay the foundation for future academic and career success.

Lower Township Elementary School District

Unit Names:

Operations and Algebraic Thinking

Numbers and Operations in Base Ten

Number and Operations - Fractions

Measurement and Data

Geometry

Materials :

GOMath! Houghton Mifflin Harcourt

Infusion of Technology :

8.1.5.A.1 Select and use the appropriate digital tools and resources to accomplish a variety of tasks including solving problems.

8.1.5.A.2 Format a document using a word processing application to enhance text and include graphics, symbols and/ or pictures.

8.1.5.A.3 Use a graphic organizer to organize information about problem or issue.

8.1.5.A.4 Graph data using a spreadsheet, analyze and produce a report that explains the analysis of the data.

8.1.P.C.1 Collaborate with peers by participating in interactive digital games or activities.

8.1.2.C.1 Engage in a variety of developmentally appropriate learning activities with students in other classes, schools, or countries using various media formats such as online collaborative tools, and social media.

Lower Township Elementary School District

Course Assessments:

District Grading Policy:

Tests

Quizzes

Homework/Classwork

Formative Assessments:

Classwork

Homework

Classroom observations

Questioning

Discussion

Personal Math Trainer

Individual whiteboards

Summative Assessments:

Chapter Assessments

End-of-year Assessment

Performance Assessments

Lower Township Elementary School District

Content Area:	Mathematics	Grade(s)	3
Unit Plan Title:	Operations and Algebraic Thinking		
Anchor Standard (ELA) or Domain (Math)			
Operations and Algebraic Thinking – 3.OA <ul style="list-style-type: none">• Represent and solve problems involving multiplication and division.• Understand properties of multiplication and the relationship between multiplication and division.• Multiply and divide within 100.• Solve problems involving the four operations, and identify and explain patterns in arithmetic.			
Overview/Rationale			
Students develop an understanding of the properties of multiplication and the relationship between multiplication and division through activities involving equal-sized groups, arrays, and area models. Students will represent and solve problems involving multiplication and division within 100. Students will solve problems involving the four operations, and identify and explain patterns in arithmetic.			
Standard(s)			
<ul style="list-style-type: none">• 3.OA.1 Interpret products of whole numbers, e.g., interpret 5×7 as the total number of objects in 5 groups of 7 objects each. For example, describe a context in which a total number of objects can be expressed as 5×7.• 3.OA.2 Interpret whole-number quotients of whole numbers, e.g., interpret $56 \div 8$ as the number of objects in each share when 56 objects are partitioned equally into 8 shares, or as a number of shares when 56 objects are partitioned into equal shares of 8 objects each. For example, describe a context in which a number of shares or a number of groups can be expressed as $56 \div 8$.• 3.OA.3 Use multiplication and division within 100 to solve word problems in situations involving equal groups, arrays, and measurement quantities, e.g., by using drawings and equations with a symbol for the unknown number to represent the problem.• 3.OA.4 Determine the unknown whole number in a multiplication or division equation relating three whole numbers. For example, determine the unknown number that makes the equation true in each of the equations $8 \times ? = 48$, $5 = \quad \div 3$, $6 \times 6 = ?$. <input type="checkbox"/>• 3.OA.5 Apply properties of operations as strategies to multiply and divide. Examples: If $6 \times 4 = 24$ is known, then $4 \times 6 = 24$ is also known. (Commutative property of multiplication.) $3 \times 5 \times 2$ can be found by $3 \times 5 = 15$, then $15 \times 2 = 30$, or by $5 \times 2 = 10$, then $3 \times 10 = 30$. (Associative property of multiplication.) Knowing that $8 \times 5 = 40$ and $8 \times 2 = 16$, one can find 8×7 as $8 \times (5 + 2) = (8 \times 5) + (8 \times 2) = 40 + 16 = 56$. (Distributive property.)• 3.OA.6 Understand division as an unknown-factor problem. For example, find $32 \div 8$ by finding the number that makes 32 when multiplied by 8.• 3.OA.7 Fluently multiply and divide within 100, using strategies such as the relationship between multiplication and division (e.g., knowing that $8 \times 5 = 40$, one knows $40 \div 5 = 8$) or properties of operations. By the end of Grade 3, know from memory all products of two one-digit numbers.			

Lower Township Elementary School District

- 3.OA.8 Solve two-step word problems using the four operations. Represent these problems using equations with a letter standing for the unknown quantity. Assess the reasonableness of answers using mental computation and estimation strategies including rounding.
- 3.OA.9 Identify arithmetic patterns (including patterns in the addition table or multiplication table), and explain them using properties of operations. For example, observe that 4 times a number is always even, and explain why 4 times a number can be decomposed into two equal addends.

Technology Standard(s)

- 8.1.5.A.1 Select and use the appropriate digital tools and resources to accomplish a variety of tasks including solving problems.**
- 8.1.5.A.2 Format a document using a word processing application to enhance text and include graphics, symbols and/ or pictures.**
- 8.1.5.A.3 Use a graphic organizer to organize information about problem or issue.**
- 8.1.5.A.4 Graph data using a spreadsheet, analyze and produce a report that explains the analysis of the data.**
- 8.1.P.C.1 Collaborate with peers by participating in interactive digital games or activities.**
- 8.1.2.C.1 Engage in a variety of developmentally appropriate learning activities with students in other classes, schools, or countries using various media formats such as online collaborative tools, and social media.**

Standards for Mathematical Practice(s)

1. Make sense of problems and persevere in solving them.
2. Reason abstractly and quantitatively.
3. Construct viable arguments and critique the reasoning of others.
4. Model with mathematics.
5. Use appropriate tools strategically.
6. Attend to precision.
7. Look for and make use of structure.
8. Look for and express regularity in repeated reasoning.

Essential Question(s)

- How can you use properties to explain patterns on the addition table?
- How can you use the strategy draw a diagram to solve one and two step addition and subtraction problems?
- How can you use equal groups to find how many in all?
- How is multiplication like addition? How is it different?
- How can you use a number line to skip count and find how many in all?
- How can you use the strategy draw a diagram to solve one and two step problems?
- How can you use arrays to model multiplication and find factors?
- How can you use the Commutative Property for Multiplication to find products?

Lower Township Elementary School District

- What happens when you multiply a number by 0 or 1?
- How can you multiply with 2 and 4?
- How can you multiply with 5 and 10?
- What are some ways to multiply with 3 and 6?
- How can you use the Distributive Property to find products?
- What strategies can you use to multiply with 7?
- How can you use the Associative Property of Multiplication to find products?
- How can you use properties to explain patterns on the multiplication table?
- What strategies can you use to multiply with 8?
- What strategies can you use to multiply with 9?
- How can you use the strategy make a table to solve multiplication problems?
- What are some ways you can describe a pattern in a table?
- How can you use an array or a multiplication table to find an unknown factor or product?
- How can you use the strategy act it out to solve problems with equal groups?
- How can you model a division problem to find how many in each group?
- How can you model a division problem to find how many equal groups?
- How can you use bar models to solve division problems?
- How is division related to subtraction?
- How can you use arrays to solve division problems?
- How can you use multiplication to divide?
- How can you write a set of related multiplication and division facts?
- What are the rules for dividing with 1 and 0?
- What does dividing by 2 mean?
- What strategies can you use to divide by 10?
- What does dividing by 5 mean?
- What strategies can you use to divide by 3?
- What strategies can you use to divide by 4?
- What strategies can you use to divide by 6?
- What strategies can you use to divide by 7?
- What strategies can you use to divide by 8?
- What strategies can you use to divide by 9?
- How can you use the strategy act it out to solve two-step problems?
- Why are there rules such as the order of operations?

Enduring Understandings

- Mathematical operations are used in solving problems in which a new value is produced from one or more values.
- Algebraic thinking involves choosing, combining, and applying effective strategies for answering quantitative questions.

Lower Township Elementary School District

In this unit plan, the following 21st Century Career Ready Practices are addressed.

Career Ready Practices	
1. Act as a responsible and contributing citizen and employee.	X
2. Apply appropriate academic and technical skills	X
3. Attend to personal health and financial well-being.	X
4. Communicate clearly and effectively and with reason.	X
5. Consider the environmental, social and economic impacts of decisions	X
6. Demonstrate creativity and innovation.	X
7. Employ valid and reliable research strategies.	X
8. Utilize critical thinking to make sense of problems and persevere in solving them.	X
9. Model integrity, ethical leadership and effective management.	X
10. Plan education and career paths aligned to personal goals.	X
11. Use technology to enhance productivity.	X
12. Work productively in teams while using cultural global competence.	X

Student Learning Targets/Objectives

- Represent and solve problems involving multiplication and division by
 - Interpreting products in multiplication (e.g., $50 = 5 \times 10$ can be interpreted as 5 groups of 10, an array with 5 rows and 10 columns, the area of a 5-by-10 rectangle, 5 rows of 10 objects).
 - Explaining division as a set of objects partitioned into an equal number of shares.
 - Identifying parts of division equations (dividend, divisor, and quotient).
 - Interpreting quotients in division (e.g., $50/10 = 5$ can be 5 groups with 10 items in each group or 10 groups with 5 items in each group).
 - Determining when to multiply and divide in word problems.
 - Representing multiplication and division word problems using drawings, and equations with unknowns in all positions.
 - Solving word problems involving equal groups, arrays, and measurement quantities using drawings and equations.
 - Determining the unknown number in multiplication and division problems such as in the following

Lower Township Elementary School District

examples: $8 \times 9 = \underline{\quad}$, $8 \times \underline{\quad} = 48$, $\underline{\quad} \times 3 = 27$, $28 \div 7 = \underline{\quad}$, $\underline{\quad} \div 6 = 3$, $35 \div \underline{\quad} = 5$.

- Understand properties of multiplication and the relationship between multiplication and division by
 - Explaining the commutative, associative, and distributive property of multiplication.
 - Applying the commutative, associative, and distributive properties to decompose, regroup, and/or reorder factors to make it easier to multiply two or more factors.
 - Explaining how the operation properties can and cannot apply to division and use those properties that can apply to make it easier to find the quotient.
 - Explaining the relationship between multiplication and division.
 - Turning a division problem into a multiplication problem with an unknown factor.
- Multiply and divide within 100 by
 - Multiplying any two numbers with a product within 100 with ease by picking and using strategies that will get to the answer fairly quickly.
 - Dividing whole numbers with a divisor within 100 and with a whole number quotient with ease by picking and using strategies that will get to the answer fairly quickly.
 - Instantly recalling from memory the product of any two one-digit numbers.
- Solve problems involving the four operations, and identify and explain patterns in arithmetic by
 - Choosing the correct operation to perform the first computation, and choosing the correct operation to perform the second computation in order to solve two-step word problems.
 - Writing equations using a letter for the unknown number.
 - Deciding if my answers are reasonable using mental math and estimation strategies including rounding.
 - Identifying and describing arithmetic patterns in number charts, addition tables, and multiplication tables.
 - Explaining arithmetic patterns using properties of operations.

Assessments

- Pre and Formative
 - Prerequisite Assessment
 - Lesson Quick Check
 - Mid-Chapter Checkpoint
 - Digital Personal Math Trainer
 - Math on the Spot Video
- Summative
 - Chapter 1 Test
 - Chapter 3 Test
 - Chapter 4 Test
 - Chapter 6 Test
 - Chapter 7 Test
- Other assessment measures
 - Show What You Know
 - Diagnostic Interview Task
 - Digital Personal Math Trainer
 - Performance Assessment Task

Chapter Review Test

Teaching and Learning Actions

Lower Township Elementary School District

<p><i>Instructional Strategies</i></p> <p>D</p>	<p><u>Instructional Strategies</u></p> <ul style="list-style-type: none"> - Breaking down the task - Differentiation strategies - Providing step-by-step prompts - Daily testing - Repeated practice - Sequenced Review - Directed Questioning and Responses - Sequence Tasks from Easy to Difficult - Individual/Small-Group/Whole Class Instruction - Think Aloud - Peer Tutoring - Active Participation - Warm-Up Activities - Meaningful Real Life Connections - Modeling - Teachers demonstrates, student uses models to problem solve - Centers - Manipulatives – Concrete Experiences - Goal Setting - Mental Math - Pencil & Paper Skills - Calculator Use/Technology - Graphic Organizers - Make Predictions/Estimation - Writing Explanations - Scaffolding - Extended Form - Partial Sums/Carrying - Trade First - Borrowing - Draw a Picture - Guess and Check - Working Backwards - Multistep
<p><i>Activities</i></p> <p>D</p>	<ul style="list-style-type: none"> • Number Sequences • Addition Top-It Game • Name That Number Game • Skip Counting on the Number Grid • Number-Grid Difference Game • Beat the Calculator Game • Guess My Coins • Fact Triangles • Ballpark Estimates • Target: 50 Game • Exploring Equal Groups

Lower Township Elementary School District

- Square Products
- Division Arrays Game
- Multiplication Songs & Tricks
- Baseball Multiplication Game
- Number Top-It Game
- Exploring Decimals
- Balls In A Container
- Multiplication Bingo Game
- Factor Bingo Game
- Roll to 100 Game
- Tic-Tac-Toe

Resources

3.OA.A.1

GoMath! Grade-3

- Lessons: 3.1-3.2

3.OA.A.2

GoMath! Grade-3

- Lessons: 6.2-6.4

3.OA.A.3

GoMath! Grade-3:

- Lessons: 3.3, 3.5, 4.1-4.3, 6.1, 6.5, 6.6, 7.1, 7.3, 7.8

3.OA.A.4

GoMath! Grade-3:

- Lessons: 5.2, 7.8

3.OA.B.5

GoMath! Grade-3:

- Lessons: 3.6-3.7, 4.4, 4.6, 6.9

3.OA.B.6

GoMath! Grade-3:

- Lessons: 6.7

3.OA.C.7

GoMath! Grade-3:

- Lessons: 4.5, 4.8, 4.9, 6.8, 7.2, 7.4-7.7, 7.9

3.OA.D.8

GoMath! Grade-3:

Lower Township Elementary School District

- Lessons: 1.12, 3.4, 4.10, 7.10, 7.11

3.OA.D.9

GoMath! Grade-3:

- Lessons: 1.1, 4.7, 4.10, 5.1

Think Central

Personal Math Trainer

GoMath! Academy

Suggested Time Frame: 54 days

Content Area:	Mathematics	Grade(s)	3
----------------------	--------------------	-----------------	----------

Unit Plan Title:	Numbers and Operations in Base Ten
-------------------------	---

Anchor Standard (ELA) or Domain (Math)

Numbers and Operations in Base Ten - 3.NBT

- Use place value understanding and properties of operations to perform multi-digit arithmetic.

Overview/Rationale

Students will develop an understanding of rounding whole numbers to the nearest 10 or 100. Using strategies based on place value and properties of operations, students will fluently add and subtract to 1000 and multiply one-digit whole numbers by multiples of 10 in the range of 10-90.

Standard(s)

- 3.NBT.1 Use place value understanding to round whole numbers to the nearest 10 or 100.
- 3.NBT.2 Fluently add and subtract within 1000 using strategies and algorithms based on place value, properties of operations, and/or the relationship between addition and subtraction.
- 3.NBT.3 Multiply one-digit whole numbers by multiples of 10 in the range 10-90 (e.g., 9×80 , 5×60) using strategies based on place value and properties of operations.

Technology Standard(s)

- 8.1.5.A.1 Select and use the appropriate digital tools and resources to accomplish a variety of tasks including solving problems.
- 8.1.5.A.2 Format a document using a word processing application to enhance text and include graphics, symbols and/ or pictures.
- 8.1.5.A.3 Use a graphic organizer to organize information about problem or issue.
- 8.1.5.A.4 Graph data using a spreadsheet, analyze and produce a report that explains the analysis of the data.
- 8.1.P.C.1 Collaborate with peers by participating in interactive digital games or activities.
- 8.1.2.C.1 Engage in a variety of developmentally appropriate learning activities with students in other classes, schools, or countries using various media formats such as online collaborative tools, and social

Lower Township Elementary School District

media.

Standards for Mathematical Practice(s)

1. Make sense of problems and persevere in solving them.
2. Reason abstractly and quantitatively.
3. Construct viable arguments and critique the reasoning of others.
4. Model with mathematics.
5. Use appropriate tools strategically.
6. Attend to precision.
7. Look for and make use of structure.
8. Look for and express regularity in repeated reasoning.

Essential Question(s)

- How can you round numbers?
- How can you use compatible numbers and rounding to estimate sums?
- How can you use compatible numbers and rounding to estimate differences?
- What mental math strategies can you use to find differences?
- How can you use place value to subtract 3-digit numbers?
- How can you use the combine place values strategy to subtract 3-digit numbers?
- What mental math strategies can you use to find sums?
- How can you add more than two addends?
- How can you use the break apart strategy to add 3-digit numbers?
- How can you use place value to add 3-digit numbers?
- How can you use a strategy draw a diagram to multiply with multiples of 10?
- What strategies can you use to multiply with multiples of 10?
- How can you model and record multiplying by 1-digit whole numbers multiples of 10?

Enduring Understandings

- Understanding place value can lead to number sense and efficient strategies for computing with numbers.

In this unit plan, the following 21st Century Career Ready Practices are addressed.

Career Ready Practices	
1. Act as a responsible and contributing citizen and employee.	X
2. Apply appropriate academic and technical skills	X
3. Attend to personal health and financial well-being.	X
4. Communicate clearly and effectively and with reason.	X

Lower Township Elementary School District

5. Consider the environmental, social and economic impacts of decisions	X
6. Demonstrate creativity and innovation.	X
7. Employ valid and reliable research strategies.	X
8. Utilize critical thinking to make sense of problems and persevere in solving them.	X
9. Model integrity, ethical leadership and effective management.	X
10. Plan education and career paths aligned to personal goals.	X
11. Use technology to enhance productivity.	X
12. Work productively in teams while using cultural global competence.	X

Student Learning Targets/Objectives

- Use place value understanding and properties of operations to perform multi-digit arithmetic by
 - Rounding whole numbers to the nearest 10.
 - Rounding whole numbers to the nearest 100.
 - Adding within 1000 with ease by using an algorithm or strategy based on place value (collecting the hundreds, collecting the tens, and collecting the ones, and when necessary, composing ten ones to make a ten or composing ten tens to make a hundred).
 - Subtracting within 1000 with ease by using an algorithm or strategy based on place value (subtracting hundreds from hundreds, tens from tens, and ones from ones, and when necessary, decomposing a hundred into ten tens or decomposing a ten into ten ones).
 - Using other strategies (such as applying the commutative or associative property, adding on to solve a subtraction problem) for adding and subtracting within 1000 with ease.
 - Multiplying one-digit numbers by 10.
 - Multiplying one-digit numbers by multiples of 10 using strategies based on place value and operation properties (e.g. $9 \times 80 = 9 \times (8 \times 10) = (9 \times 8) \times 10$; or $9 \times 80 = (9 \times 50) + (9 \times 30)$).

Assessments

- Pre and Formative
 - Prerequisite Assessment
 - Lesson Quick Check
 - Mid-Chapter Checkpoint
 - Digital Personal Math Trainer
 - Math on the Spot Video
- Summative
 - Chapter 1 Test
 - Chapter 5 Test
- Other assessment measures
 - Show What You Know

Lower Township Elementary School District

- Diagnostic Interview Task
- Digital Personal Math Trainer
- Performance Assessment Task
- Chapter Review Test

Teaching and Learning Actions

<p><i>Instructional Strategies</i></p> <p>D</p>	<p><u>Instructional Strategies</u></p> <ul style="list-style-type: none"> - Breaking down the task - Differentiation strategies - Providing step-by-step prompts - Daily testing - Repeated practice - Sequenced Review - Directed Questioning and Responses - Sequence Tasks from Easy to Difficult - Individual/Small-Group/Whole Class Instruction - Think Aloud - Peer Tutoring - Active Participation - Warm-Up Activities - Meaningful Real Life Connections - Modeling - Teachers demonstrates, student uses models to problem solve - Centers - Manipulatives – Concrete Experiences - Goal Setting - Mental Math - Pencil & Paper Skills - Calculator Use/Technology - Graphic Organizers - Make Predictions/Estimation - Writing Explanations - Scaffolding - Extended Form - Partial Sums/Carrying - Trade First - Borrowing - Draw a Picture - Guess and Check - Working Backwards - Multistep
<p><i>Activities</i></p> <p>D</p>	<ul style="list-style-type: none"> ● Less Than You! Game ● Addition Top-It Game ● Skip Counting on the Number Grid ● Number-Grid Difference Game ● Beat the Calculator Game ● Guess My Coins

Lower Township Elementary School District

	<ul style="list-style-type: none">• Name That Number Game• Fact Triangles• “What’s My Rule?”• Ballpark Estimates• Target: 50 Game• Multiplication Songs & Tricks• Baseball Multiplication Game• 5-Digit Place Value Chart• Number Diagram• Number Top-It Game• Number Top-It Through Millions Game• Multiplication Bingo Game• Roll to 100 Game• Field Trip Planner
Resources	
<p>3.NBT.A.1 GoMath! Grade-3: • Lessons: 1.2-1.3, 1.8</p> <p>3.NBT.A.2 GoMath! Grade-3: • Lessons: 1.4-1.7, 1.9-1.11 •</p> <p>3.NBT.A.3 GoMath! Grade-3: • Lessons: 5.3-5.5</p> <p>Think Central</p> <p>Personal Math Trainer</p> <p>GoMath! Academy</p>	
Suggested Time Frame:	18 days

Lower Township Elementary School District

Content Area:	Mathematics	Grade(s)	3
Unit Plan Title:	Numbers and Operations - Fractions		
Anchor Standard (ELA) or Domain (Math)			
Numbers and Operations – Fractions – 3.NF <ul style="list-style-type: none">Develop understanding of fractions as numbers.			
Overview/Rationale			
<p>Students develop an understanding of fractions, beginning with unit fractions. Visual fraction models, including the introductory unit fraction, are used to represent parts of a whole. Students understand that the size of a fractional part is relative to the size of the whole. For example, $\frac{1}{2}$ of the paint in a small bucket could be less paint than $\frac{1}{3}$ of the paint in a larger bucket, but $\frac{1}{3}$ of a ribbon is longer than $\frac{1}{5}$ of the same ribbon because when the ribbon is divided into 3 equal parts, the parts are longer than when the ribbon is divided into 5 equal parts. Students are able to use fractions to represent numbers equal to, less than, and greater than one. They solve problems that involve comparing fractions by using visual fraction models and strategies based on noticing equal numerators or denominators.</p>			
Standard(s)			
<ul style="list-style-type: none">3.NF.1 Understand a fraction $\frac{1}{b}$ as the quantity formed by 1 part when a whole is partitioned into b equal parts; understand a fraction $\frac{a}{b}$ as the quantity formed by a parts of size $\frac{1}{b}$.3.NF.2 Understand a fraction as a number on the number line; represent fractions on a number line diagram.<ol style="list-style-type: none">Represent a fraction $\frac{1}{b}$ on a number line diagram by defining the interval from 0 to 1 as the whole and partitioning it into b equal parts. Recognize that each part has size $\frac{1}{b}$ and that the endpoint of the part based at 0 locates the number $\frac{1}{b}$ on the number line.Represent a fraction $\frac{a}{b}$ on a number line diagram by marking off a lengths $\frac{1}{b}$ from 0. Recognize that the resulting interval has size $\frac{a}{b}$ and that its endpoint locates the number $\frac{a}{b}$ on the number line.3.NF.3 Explain equivalence of fractions in special cases, and compare fractions by reasoning about their size.<ol style="list-style-type: none">Understand two fractions as equivalent (equal) if they are the same size, or the same point on a number line.Recognize and generate simple equivalent fractions, e.g., $\frac{1}{2} = \frac{2}{4}$, $\frac{4}{6} = \frac{2}{3}$. Explain why the fractions are equivalent, e.g., by using a visual fraction model.Express whole numbers as fractions, and recognize fractions that are equivalent to whole numbers. Examples: Express 3 in the form $3 = \frac{3}{1}$; recognize that $\frac{6}{1} = 6$; locate $\frac{4}{4}$ and 1 at the same point of a number line diagram.Compare two fractions with the same numerator or the same denominator by reasoning about their size. Recognize that comparisons are valid only when the two fractions refer to the same whole. Record the results of comparisons with			

Lower Township Elementary School District

the symbols $>$, $=$, or $<$, and justify the conclusions, e.g., by using a visual fraction model.

Technology Standard(s)

- 8.1.5.A.1** Select and use the appropriate digital tools and resources to accomplish a variety of tasks including solving problems.
- 8.1.5.A.2** Format a document using a word processing application to enhance text and include graphics, symbols and/ or pictures.
- 8.1.5.A.3** Use a graphic organizer to organize information about problem or issue.
- 8.1.5.A.4** Graph data using a spreadsheet, analyze and produce a report that explains the analysis of the data.
- 8.1.P.C.1** Collaborate with peers by participating in interactive digital games or activities.
- 8.1.2.C.1** Engage in a variety of developmentally appropriate learning activities with students in other classes, schools, or countries using various media formats such as online collaborative tools, and social media.

Standards for Mathematical Practice(s)

1. Make sense of problems and persevere in solving problems.
2. Reason abstractly and quantitatively.
3. Construct viable arguments and critique the reasoning of others.
4. Model with mathematics.
5. Use appropriate tools strategically.
6. Attend to precision.
7. Look for and make use of structure.
8. Look for and express regularity in repeated reasoning.

Essential Question(s)

- What are equal parts of a whole?
- Why do you need to know how to make equal shares?
- What do the top and bottom numbers of a fraction tell?
- How does a fraction name part of a whole?
- How can you represent and locate fractions on a number line?
- When might you use a fraction greater than 1 or a whole number?
- How can a fraction name part of a group?

- How can a fraction tell how many are in part of a group?
- How can you use the strategy draw a diagram to solve fraction problems?
- How can you use the strategy act it out to solve comparison problems?

Lower Township Elementary School District

- How can you compare fractions with the same denominator?
- How can you compare fractions with the same numerator?
- What strategies can you use to compare fractions?
- How can you compare and order fractions?
- How can you use models to find equivalent fractions?
- How can you use models to name equivalent fractions?

Enduring Understandings

- Fractions and decimals allow for quantities to be expressed with greater precision than with just whole numbers.

In this unit plan, the following 21st Century Career Ready Practices are addressed.

Career Ready Practices	
1. Act as a responsible and contributing citizen and employee.	X
2. Apply appropriate academic and technical skills	X
3. Attend to personal health and financial well-being.	X
4. Communicate clearly and effectively and with reason.	X
5. Consider the environmental, social and economic impacts of decisions	X
6. Demonstrate creativity and innovation.	X
7. Employ valid and reliable research strategies.	X
8. Utilize critical thinking to make sense of problems and persevere in solving them.	X
9. Model integrity, ethical leadership and effective management.	X
10. Plan education and career paths aligned to personal goals.	X
11. Use technology to enhance productivity.	X
12. Work productively in teams while using cultural global competence.	X

Student Learning Targets/Objectives

- Develop understanding of fractions as numbers by
 - Explaining any unit fraction ($1/b$) as one part of a whole.
 - Explaining any fraction (a/b) as “a” (numerator) being the numbers of parts and “b” (denominator) as

Lower Township Elementary School District

the total number of equal parts in the whole.

- Explaining and showing how $1/b$ can be represented on a number line in two ways: (1) as a number that is located a distance of $1/b$ to the right of 0, and (2) as the size of each of the parts when a whole is partitioned into b equal parts.
- Explaining and showing how a/b can be represented on a number line in two ways: (1) as a number that is located a distance of a/b to the right of 0, and (2) as the size of a parts when a whole is partitioned into b equal parts.
- Representing a unit fraction ($1/b$) on a number line between 0 and 1.
- Representing any fraction (a/b) on a number line.
- Using models to show and explain equivalent fractions.
- Locating equivalent fractions on a number line.
- Using models to show and explain whole numbers as fractions.
- Locating whole numbers as fractions on a number line.
- Using models to compare two fractions and record the comparison using $>$, $<$, or $=$.
- Explaining how the size of equal parts can be used to compare two fractions with the same numerator, and explaining how the number of equal parts can be used to compare fractions with the same denominator.

Assessments

- Pre and Formative
 - Prerequisite Assessment
 - Lesson Quick Check
 - Mid-Chapter Checkpoint
 - Digital Personal Math Trainer
 - Math on the Spot Video
- Summative
 - Chapter 8 Test
 - Chapter 9 Test
- Other assessment measures
 - Show What You Know
 - Diagnostic Interview Task
 - Digital Personal Math Trainer
 - Performance Assessment Task
 - Chapter Review Test

Teaching and Learning Actions

<p><i>Instructional Strategies</i></p> <p>D</p>	<p><u>Instructional Strategies</u></p> <ul style="list-style-type: none"> - Breaking down the task - Differentiation strategies - Providing step-by-step prompts - Daily testing - Repeated practice - Sequenced Review - Directed Questioning and Responses - Sequence Tasks from Easy to Difficult
--	---

Lower Township Elementary School District

	<ul style="list-style-type: none"> - Individual/Small-Group/Whole Class Instruction - Think Aloud - Peer Tutoring - Active Participation - Warm-Up Activities - Meaningful Real Life Connections - Modeling - Teachers demonstrates, student uses models to problem solve - Centers - Manipulatives – Concrete Experiences - Goal Setting - Mental Math - Pencil & Paper Skills - Calculator Use/Technology - Graphic Organizers - Make Predictions/Estimation - Writing Explanations - Scaffolding - Extended Form - Partial Sums/Carrying - Trade First - Borrowing - Draw a Picture - Guess and Check - Working Backwards - Multistep
<p><i>D</i></p> <p style="text-align: center;"><i>Activities</i></p>	<ul style="list-style-type: none"> • Name That Number Game • Rulers • Exploring Decimals • Beat the Calculator Game • Number Top-It (Decimals) Game • Math Messages • Balls In A Container • Fraction Cards • Equivalent Fractions Game • The Block-Drawing Game • Fraction Top-It Game • Tic-Tac-Toe
Resources	
<p>3.NF.1 GoMath! Grade 3:</p> <ul style="list-style-type: none"> • Lessons: 8.1-8.4, 8.7-8.9 <p>3.NF.2 GoMath! Grade 3:</p> <ul style="list-style-type: none"> • Lessons: 8.5 	

Lower Township Elementary School District

3.NF.3

GoMath! Grade 3:

- Lessons: 8.6, 9.1-9.7

Think Central

Personal Math Trainer

GoMath! Academy

Suggested Time Frame:

31 days

Content Area:	Mathematics	Grade(s)	3
Unit Plan Title:	Measurement and Data		
Anchor Standard (ELA) or Domain (Math)			
<p>Measurement and Data – 3.MD</p> <ul style="list-style-type: none"> • Solve problems involving measurement and estimation of intervals of time, liquid volumes, and masses of objects. • Represent and interpret data. • Geometric measurement: understand concepts of area and relate area to multiplication and to addition. • Geometric measurement: recognize perimeter as an attribute of plane figures and distinguish between linear and area measures. 			
Overview/Rationale			
<p>Students recognize area as an attribute of two-dimensional regions. Area of a shape is measured by finding the total number of same-size units of area required to cover the shape without gaps or overlaps, a square with sides of unit length being the standard unit for measuring area. Students understand that rectangular arrays can be decomposed into identical rows or into identical columns. By decomposing rectangles into rectangular arrays, students relate area to multiplication and to addition. Students solve problems involving measurement and estimation of intervals of time, liquid volumes, and masses of objects.</p>			
Standard(s)			

Lower Township Elementary School District

- 3.MD.1 Tell and write time to the nearest minute and measure time intervals in minutes. Solve word problems involving addition and subtraction of time intervals in minutes, e.g., by representing the problem on a number line diagram.
- 3.MD.2 Measure and estimate liquid volumes and masses of objects using standard units of grams (g), kilograms (kg), and liters (l). Add, subtract, multiply, or divide to solve one-step word problems involving masses or volumes that are given in the same units, e.g., by using drawings (such as a beaker with a measurement scale) to represent the problem.
- 3.MD.3 Draw a scaled picture graph and a scaled bar graph to represent a data set with several categories. Solve one- and two-step “how many more” and “how many less” problems using information presented in scaled bar graphs. For example, draw a bar graph in which each square in the bar graph might represent 5 pets.
- 3.MD.4 Generate measurement data by measuring lengths using rulers marked with halves and fourths of an inch. Show the data by making a line plot, where the horizontal scale is marked off in appropriate units – whole numbers, halves, or quarters.
- 3.MD.5 Recognize area as an attribute of plane figures and understand concepts of area measurement.
 - a. A square with side length 1 unit, called “a unit square,” is said to have “one square unit” of area, and can be used to measure area.
 - b. A plane figure which can be covered without gaps or overlaps by n unit squares is said to have an area of n square units.
- 3.MD.6 Measure areas by counting unit squares (square cm, square m, square in, square ft, and improvised units).
- 3.MD.7 Relate area to the operations of multiplication and addition.
 - a. Find the area of a rectangle with whole-number side lengths by tiling it, and show that the area is the same as would be found by multiplying the side lengths.
 - b. Multiply side lengths to find areas of rectangles with whole-number side lengths in the context of solving real world and mathematical problems, and represent whole-number products as rectangular areas in mathematical reasoning.
 - c. Use tiling to show in a concrete case that the area of a rectangle with whole-number side lengths a and $b + c$ is the sum of $a \times b$ and $a \times c$. Use area models to represent the distributive property in mathematical reasoning.
 - d. Recognize area as additive. Find areas of rectilinear figures by decomposing them into non-overlapping rectangles and adding the areas of the non-overlapping parts, applying this technique to solve real world problems.
- 3.MD.8 Solve real world and mathematical problems involving perimeters of polygons, including finding the perimeter given the side lengths, finding an unknown side length, and exhibiting rectangles with the same perimeter and different areas or with the same area and different perimeters.

Technology Standard(s)

- 8.1.5.A.1 Select and use the appropriate digital tools and resources to accomplish a variety of tasks including solving problems.**
- 8.1.5.A.2 Format a document using a word processing application to enhance text and include graphics,**

Lower Township Elementary School District

symbols and/ or pictures.

8.1.5.A.3 Use a graphic organizer to organize information about problem or issue.

8.1.5.A.4 Graph data using a spreadsheet, analyze and produce a report that explains the analysis of the data.

8.1.P.C.1 Collaborate with peers by participating in interactive digital games or activities.

8.1.2.C.1 Engage in a variety of developmentally appropriate learning activities with students in other classes, schools, or countries using various media formats such as online collaborative tools, and social media.

Standards for Mathematical Practice(s)

1. Make sense of problems and persevere in solving problems.
2. Reason abstractly and quantitatively.
3. Construct viable arguments and critique the reasoning of others.
4. Model with mathematics.
5. Use appropriate tools strategically.
6. Attend to precision.
7. Look for and make use of structure.
8. Look for and express regularity in repeated reasoning.

Essential Question(s)

- How can you use the strategy make a table to organize data and solve problems?
- How can you read and interpret data in a picture graph?
- How can you draw a picture graph to show data in a table?
- How can you read and interpret data in a bar graph?
- How can you draw a bar graph to show data in a table or picture graph?
- How can you solve problems using data represented in bar graphs?
- How can you read and interpret data in a line plot and use data to make a line plot?
- How can you tell time to the nearest minute?
- How can you tell when to use A.M. and P.M. with time?
- How can you measure elapsed time in minutes?
- How can you find a starting time or an ending time when you know the elapsed time?
- How can you use the strategy draw a diagram to solve problems about time?
- How can you generate measurement data and show the data on a line plot?
- How can you estimate and measure liquid volume in metric units?
- How can you estimate and measure mass in metric units?
- How can you use models to solve liquid volume and mass problems?
- How can you find perimeter?
- How can you measure perimeter?
- How can you find the unknown length of a side in a plane figure when you know its perimeter?
- How is finding the area of a figure different from finding the perimeter of a figure?
- How can you find the area of a plane figure?
- Why can you multiply to find the area of a rectangle?
- How can you use the strategy find a pattern to solve area problems?
- How can you break apart a figure to find the area?

Lower Township Elementary School District

- How can you use area to compare rectangles with the same perimeter?
- How can you use perimeter to compare rectangles with the same area?

Enduring Understandings

- Measurement processes are used in everyday life to describe and quantify the world.
- Data displays describe and represent data in alternative ways.

In this unit plan, the following 21st Century Career Ready Practices are addressed.

Career Ready Practices	
1. Act as a responsible and contributing citizen and employee.	X
2. Apply appropriate academic and technical skills	X
3. Attend to personal health and financial well-being.	X
4. Communicate clearly and effectively and with reason.	X
5. Consider the environmental, social and economic impacts of decisions	X
6. Demonstrate creativity and innovation.	X
7. Employ valid and reliable research strategies.	X
8. Utilize critical thinking to make sense of problems and persevere in solving them.	X
9. Model integrity, ethical leadership and effective management.	X
10. Plan education and career paths aligned to personal goals.	X
11. Use technology to enhance productivity.	X
12. Work productively in teams while using cultural global competence.	X

Student Learning Targets/Objectives

- Solve problems involving measurement and estimation of intervals of time, liquid volumes, and masses of objects by
 - Saying and writing time to the nearest minute.
 - Measuring a duration of time in minutes (e.g., basketball practice is 45 minutes long).
 - Solving addition and subtraction word problems involving durations of time measured in minutes.
 - Estimating liquid volumes and masses of objects using standard units of measure (grams, kilograms, and liters).
 - Measuring liquid volumes and masses of objects using standard units of measure (grams, kilograms, and liters).
 - Using a drawing to represent one-step word problems involving masses or volumes.

Lower Township Elementary School District

- Solving one-step word problems involving masses or volumes using addition, subtraction, multiplication, or division.
- Represent and interpret data by
 - Making a scaled picture graph or bar graph with several categories to represent data (e.g., one square or picture represents 5 objects).
 - Reading and interpreting scaled bar graphs in order to solve one- and two-step “how many more” and “how many less” problems.
 - Using a ruler to measure lengths in whole, half, and quarter inches.
 - Gathering and recording measurement data using whole, half, and quarter inches.
 - Making a line plot with the horizontal scale marked off in whole number, half, or quarter units.
- Geometric measurement: understand concepts of area and relate area to multiplication and to addition by
 - Defining a unit square.
 - Defining area as the measure of space with a plane figure and explain why area is measured in square units.
 - Measuring the area of a shape or flat surface by covering it with unit squares – with no gaps or overlaps – and counting the number of unit squares used.
 - Using tiles to find the area of rectangles.
 - Explaining the relationship between tiling and multiplying side lengths to find the area of rectangles.
 - Multiplying adjacent side lengths of rectangles to solve word problems.
 - Using area models to explain the distributive property.
 - Decomposing an irregular figure into non-overlapping rectangles.
 - Explaining area as additive and use this understanding to solve word problems.
- Geometric measurement: recognize perimeter as an attribute of plane figures and distinguish between linear and area measures by
 - Identifying polygons.
 - Defining perimeter.
 - Finding the perimeter of polygons when given the lengths of all sides.
 - Finding unknown side lengths of polygons when given the perimeter.
 - Showing how rectangles with the same perimeter can have different areas and showing rectangles with the same area can have different perimeters.
 - Solving word problems involving perimeter.

Assessments

- Pre and Formative
 - Prerequisite Assessment
 - Lesson Quick Check
 - Mid-Chapter Checkpoint
 - Digital Personal Math Trainer
 - Math on the Spot Video
- Summative
 - Chapter 2 Test
 - Chapter 10 Test
 - Chapter 11 Test
- Other assessment measures

Lower Township Elementary School District

- Show What You Know
 - Diagnostic Interview Task
 - Digital Personal Math Trainer
 - Performance Assessment Task
- Chapter Review Test

Teaching and Learning Actions

<p><i>Instructional Strategies</i></p> <p><i>D</i></p>	<p><u>Instructional Strategies</u></p> <ul style="list-style-type: none"> - Breaking down the task - Differentiation strategies - Providing step-by-step prompts - Daily testing - Repeated practice - Sequenced Review - Directed Questioning and Responses - Sequence Tasks from Easy to Difficult - Individual/Small-Group/Whole Class Instruction - Think Aloud - Peer Tutoring - Active Participation - Warm-Up Activities - Meaningful Real Life Connections - Modeling - Teachers demonstrates, student uses models to problem solve - Centers - Manipulatives – Concrete Experiences - Goal Setting - Mental Math - Pencil & Paper Skills - Calculator Use/Technology - Graphic Organizers - Make Predictions/Estimation - Writing Explanations - Scaffolding - Extended Form - Partial Sums/Carrying - Trade First - Borrowing - Draw a Picture - Guess and Check - Working Backwards - Multistep
<p><i>Activities</i></p> <p><i>D</i></p>	<ul style="list-style-type: none"> ● Addition Top-It Game ● Math Boxes ● Guess My Coins ● Name That Number Game ● Subtraction Top-It Game

Lower Township Elementary School District

- Area Grids
- Square Products
- Division Arrays Game
- Number Top-It (5-Digit Numbers) Game
- Number Top-It Game
- Number Top-It (7-Digit Numbers) Game
- Beat the Calculator Game
- Exploring Decimals
- Number Top-It (Decimals) Game
- Constructing a Flipbook
- Baseball Multiplication Game
- Constructing a Vocabulary Chart
- Roll to 100 Game
- Field Trip Planner

Resources

3.MD.1

GoMath! Grade 3:

- Lessons: 10.1-10.5

3.MD.2

GoMath! Grade 3:

- Lessons: 10.7-10.9

3.MD.4

GoMath! Grade 3:

- Lessons: 10.6, 11.4

3.MD.5

GoMath! Grade 3:

- Lessons: 11.5

3.MD.7

GoMath! Grade 3:

- Lessons: 11.6-11.8

3.MD.8

GoMath! Grade 3:

- Lessons: 11.1-11.3, 11.9-11.10

3.MD.B.3

GoMath! Grade 3:

Lower Township Elementary School District

- Lessons: 2.1-2.6

3.MD.B.4

GoMath! Grade 3:

- Lessons: 2.7

Think Central

Personal Math Trainer

GoMath! Academy

Suggested Time Frame:

35 days

Lower Township Elementary School District

Content Area:	Mathematics	Grade(s)	3
Unit Plan Title:	Geometry		
Anchor Standard (ELA) or Domain (Math)			
Geometry – 3.G <ul style="list-style-type: none"> • Reason with shapes and their attributes. 			
Overview/Rationale			
<p>Students reason with shapes and their attributes by describing, analyzing, and comparing properties of two-dimensional shapes. Students will formulate understanding by comparing and classifying shapes by their sides and angles, and connecting these with definitions of shapes. Fractions and geometry are connected by expressing the area of part of a shape as a unit fraction of the whole.</p>			
Standard(s)			
<ul style="list-style-type: none"> • 3.G.1 Understand that shapes in different categories (e.g., rhombuses, rectangles, and others) may share attributes (e.g., having four sides), and that the shared attributes can define a larger category (e.g., quadrilaterals). Recognize rhombuses, rectangles, and squares as examples of quadrilaterals, and draw examples of quadrilaterals that do not belong to any of these subcategories. • 3.G.2 Partition shapes into parts with equal areas. Express the area of each part as a unit fraction of the whole. For example, partition a shape into 4 parts with equal area, and describe the area of each part as $\frac{1}{4}$ of the area of the shape. 			
<u>Technology Standard(s)</u>			
<p>8.1.5.A.1 Select and use the appropriate digital tools and resources to accomplish a variety of tasks including solving problems.</p> <p>8.1.5.A.2 Format a document using a word processing application to enhance text and include graphics, symbols and/ or pictures.</p> <p>8.1.5.A.3 Use a graphic organizer to organize information about problem or issue.</p> <p>8.1.5.A.4 Graph data using a spreadsheet, analyze and produce a report that explains the analysis of the data.</p> <p>8.1.P.C.1 Collaborate with peers by participating in interactive digital games or activities.</p> <p>8.1.2.C.1 Engage in a variety of developmentally appropriate learning activities with students in other classes, schools, or countries using various media formats such as online collaborative tools, and social media.</p>			
<u>Standards for Mathematical Practice(s)</u>			
<ol style="list-style-type: none"> 1. Make sense of problems and persevere in solving problems. 2. Reason abstractly and quantitatively. 3. Construct viable arguments and critique the reasoning of others. 4. Model with mathematics. 5. Use appropriate tools strategically. 6. Attend to precision. 			

Lower Township Elementary School District

- 7. Look for and make use of structure.
- 8. Look for and express regularity in repeated reasoning.

Essential Question(s)

- What are some ways to describe two-dimensional shapes?
- How can you describe angles in plane shapes?
- How can you use line segments and angles to make polygons?
- How can you describe line segments that are sides of polygons?
- How can you use sides and angles to help you describe quadrilaterals?
- How can you draw quadrilaterals?
- How can you use sides and angles to help you describe triangles?
- How can you use the strategy draw a diagram to classify plane shapes?
- How can you divide shapes into parts and equal areas and write the area as a unit fraction of the whole?

Enduring Understandings

- Geometric attributes (such as shapes, lines, angles, figures, and planes) provide descriptive information about an object’s properties and position in space and support visualization and problem solving.

In this unit plan, the following 21st Century Career Ready Practices are addressed.

Career Ready Practices	
1. Act as a responsible and contributing citizen and employee.	X
2. Apply appropriate academic and technical skills	X
3. Attend to personal health and financial well-being.	X
4. Communicate clearly and effectively and with reason.	X
5. Consider the environmental, social and economic impacts of decisions	X
6. Demonstrate creativity and innovation.	X
7. Employ valid and reliable research strategies.	X
8. Utilize critical thinking to make sense of problems and persevere in solving them.	X
9. Model integrity, ethical leadership and effective management.	X
10. Plan education and career paths aligned to personal goals.	X
11. Use technology to enhance productivity.	X
12. Work productively in teams while using cultural global	X

Lower Township Elementary School District

competence.

Student Learning Targets/Objectives

- Reason with shapes and their attributes by
 - Using attributes to identify shapes.
 - Using attributes to classify shapes into categories.
 - Defining quadrilaterals.
 - Recognizing rhombuses, rectangles, and squares as being examples of quadrilaterals.
 - Drawing quadrilaterals other than rhombuses, rectangles, and squares.
 - Partitioning (dividing) shapes into equal parts with equal areas.
 - Explaining any unit fraction ($1/b$) as one part of a whole divided into b equal parts (e.g., $1/2$, $1/4$, $1/8$).

Assessments

- Pre and Formative
 - Prerequisite Assessment
 - Lesson Quick Check
 - Mid-Chapter Checkpoint
 - Digital Personal Math Trainer
 - Math on the Spot Video
- Summative
 - Chapter 12 Test
 - Other assessment measures
 - Show What You Know
 - Diagnostic Interview Task
 - Digital Personal Math Trainer
 - Performance Assessment Task
 - Chapter Review Test

Teaching and Learning Actions

Instructional Strategies
D

Instructional Strategies

- Breaking down the task
- Differentiation strategies
- Providing step-by-step prompts
- Daily testing
- Repeated practice
- Sequenced Review
- Directed Questioning and Responses
- Sequence Tasks from Easy to Difficult
- Individual/Small-Group/Whole Class Instruction
- Think Aloud
- Peer Tutoring
- Active Participation
- Warm-Up Activities
- Meaningful Real Life Connections
- Modeling - Teachers demonstrates, student uses models to problem solve
- Centers

Lower Township Elementary School District

	<ul style="list-style-type: none"> - Manipulatives – Concrete Experiences - Goal Setting - Mental Math - Pencil & Paper Skills - Calculator Use/Technology - Graphic Organizers - Make Predictions/Estimation - Writing Explanations - Scaffolding - Extended Form - Partial Sums/Carrying - Trade First - Borrowing - Draw a Picture - Guess and Check - Working Backwards - Multistep
<i>D</i> <i>Activities</i>	<ul style="list-style-type: none"> • Math Boxes • Constructing a Vocabulary Chart • Angle Race Game • The Block-Drawing Game
Resources	
<p>3.G.1 GoMath! Grade 3:</p> <ul style="list-style-type: none"> • Lessons: 12.1-12.8 <p>3.G.2 GoMath! Grade 3:</p> <ul style="list-style-type: none"> • Lessons: 12.9 	
Suggested Time Frame:	13 days

Lower Township Elementary School District